# Do Maternal Health Problems Influence Child's Worrying Status? Evidence from British Cohort Study

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#### Abstract

The influence of maternal health problems on child's worrying status is important in practice in terms of the intervention of maternal health problems early for the influence on child's worrying status. Conventional methods apply symmetric prior distributions such as a normal distribution or a Laplace distribution for regression coefficients, which may be suitable for median regression and exhibit no robustness to outliers. This work develops a quantile regression on linear panel data model without heterogeneity from a Bayesian point of view, i.e., upon a location-scale mixture representation of the asymmetric Laplace error distribution, this work provides how the posterior distribution can be sampled and summarized by Markov chain Monte Carlo method. Applying this approach to the 1970 British Cohort Study data, it finds that a different maternal health problem has different influence on child's worrying status at different quantiles. In addition, applying stochastic search variable selection for maternal health problems to the 1970 British Cohort Study data, it finds that maternal nervous breakdown, in this work, among the 25 maternal health problems, contributes most to influence the child's worrying status.

Key words: British Cohort Study data; Bayesian inference; Quantile regression; Asymmetric Laplace error distribution; Markov chain Monte Carlo; Variable selection. JEL classification: C11, C38, C63.

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## 1 Introduction

In many applications, conventional regression analysis addressed much attention and focuses on the mean effect or optimal forecasting in a mean squared error sense. Since a set of quantles often provides more complete description of the response distribution than the mean, over classical mean regression, quantile regression not only quantifies the relationship between quantiles of the response distribution and covariates, but also exhibits robustness to outliers and has a wide applicability (Buchinsky, 1998; Yu et al., 2003; and Koenker, 2005). Quantile regression has been applied in many areas, for example, to calculate Value at Risk and expected shortfall for financial risk management (Taylor, 2008), to study the relationship between GDP and population (Schnabel and Eilers, 2009), to study the correlation of the wage and the level of education (Härdle and Song, 2010), and to estimate the volatility of temperatures (Guo and Härdle (2012).

For classical quantile regression, the error distribution is often assumed to have the p-th quantile equal to zero, see, for example, Yu and Stander (2007), and classical qantile regression parameters depend on asymptotic normality which is assumed unbiased and normal. Inaddition, confidence intervals depends on the density function of model error which is difficult to estimate reliability. On the contrary, credible intervals from Bayesian inference can avoid these problems, whatever sample sizes. Aside from these, Bayesian inference can take historical information or expert opinion easily via prior information. Therefore Bayesian quantile regression is naturally motivated.

Quantile regression is attempted in Bayesian framework in both theoretical and applied econometric analysis, for example, Walker and Mallick (1999), Kottas and Gelfand (2001), and Hanson and Johnson (2002) on median regression (one special quantile regression), and Yu and Moyeed (2001), Tsionas (2003) and Kozumi and Kobayashi (2010) on general quantile regression with the asymmetric Laplace density for the errors. In addition, on infinite mixture model, Kottas and Krnjajic (2009) on Bayesian semi-parametric approach, Yu (2002), Taddy and Kottas (2010) and Yue and Rue (2011) on Bayesian nonparametric approach. However, few studies have been on Bayesian quantile regression for panel data (Yuan and Yin, 2010; Reich et al., 2010).

This paper develops a Bayesian quantile regression for linear panel data without heterogeneity. For posterior inference, upon a location-scale mixture representation of the asymmetric Laplace error distribution, we propose a Gibbs sampling algorithm and develop Markov chain Monte Carlo (MCMC) methods (see, e.g., Chib 2001; Liu 2001; Gamerman and Lopes 2006). All posterior densities are fully tractable and easy to sample, making the Gibbs sampler appealing when several quantile regressions are required at one time. In addition, the proposed Gibbs sampler can be applied for the calculation of the marginal likelihood and the variable selection.

For variable selection, several criteria have been proposed (see, for example, Zwick and Velicer, 1986), though no agreement has emerged in the literature on optimal criterion. Aside from the classical literature, Bayesian approach focus on an unknown number of variables (Frühwirth-Schnatter and Lopes, 2009). Variable selection in modeling with Bayesian quantile regression is difficult due to the computational efficiency. This work applies stochastic search variable selection based on Markov chain Monte Carlo method.

We apply Bayesian approach to the 1970 British Cohort Study (BCS) to analyze the influence of maternal health problems on child's worrying status. This is the first instance, as we know, in which the influences of maternal health problems are estimated to account for child's worrying status. We find that different maternal health problems have different influence on child's worrying status at different quantiles, and find that maternal nervous breakdown, in our method, among the 25 maternal health problems, contributes most to influence the child's worrying status.

This paper joins the literature in health economics and personality psychology. While

it is established in psychology on their importance (see, for example, Roberts et al., 2006, 2007; Hampson and Friedman, 2008), and in economics for the influence of personality traits on health (Kaestner and Callison, 2011; Conti et al., 2010) and health-related behaviors (Heckman et al., 2006; Cutler and Lleras-Muney, 2010; Conti et al., 2010), it is less recognized in economics on the influence of maternal health problems on child's worrying status.

Using principal component analysis, a few studies using the BCS data can be found in the economic literature. Blanden et al. (2007) constructs several non-cognitive measures to analyze their role in explaining the rise in intergenerational income persistence across the 1958 and the 1970 cohorts. Feinstein (2000) constructs several indicators of psychological and behavioral development to analyze their effects on education and labor market outcomes. Murasko (2007) computes the standardized raw scores from the locus of control and selfesteem scales and finds that both are significant predictors of self-reported poor health at age 30. This analysis goes beyond those studies, as we apply Bayesian inference and variable selection to examine the influence of maternal health problems on child's worrying status.

Our work contributes an important methodological advancement to these literatures. When in a data-rich environment, researchers used traditional methods to estimate and select variables, and in many cases they have been limited by the computing challenging. Using the BCS data, we propose Bayesian inference and apply variable selection in this paper, and find that maternal's different health problems have different influence on child's worrying status at different quantiles, and that maternal nervous breakdown, in our method, among the 25 maternal health problems, contributes most to influence the child's worrying status.

The paper is structured as follows. In the next section, we describe the BCS data. Section 3 outlines the basic model, while Section 4 develops MCMC method for quantile regression model and explain how the MCMC output may be used to compute the marginal likelihoods and for variable selection. Empirical implementation and results for our Bayesian approach are shown in Section 5. Section 6 concludes our findings.

## 2 Data: The British Cohort Study

The data, we use in this paper, are from the BCS, a survey of all babies born (alive or dead) after the 24-th week of gestation from 00.01 hours on Sunday, 5th April to 24.00 hours on Saturday, 11 April, 1970 in places including England, Scotland, Wales and Northern Ireland. Seven surveys, in detail, respectively in 1975, 1980, 1986, 1996, 2000, 2004 and 2008, are followed up so far to trace all members of the birth cohort. Information on background characteristics is drawn from the survey in 1975 and 1980 on maternal health problems, and on child's worrying status from the survey in 1980 and 1986. Samples from the family of multiple children are excluded for the reason of peer effect, and samples for the respondents with any missing information on those background characteristics are also excluded. A sample of size 3,426 is left for our analysis in this paper.

#### 2.1 Rutter Score Derived Variable for Child

Applying the Rutter Behaviour Scale question "Often worried?" for child, the Rutter score derived variable, Y, was derived, where the question was completed by the cohort member's parent (usually the mother) in the BCS 1980 and 1986 follow-up data sets. For our case, the discrete choice results from 1 (Does not worried), 2 (Somewhat worried), 3 (Certainly worried).

#### 2.2 Mother Malaise Score Derived Variables

Applying the Malaise Inventory ("How you feel") completed by the cohort member's parent (usually the mother), the mother malaise score derived variables were derived on behalf of the cohort member and included in the BCS 1975 and 1980 follow-up data sets. These 25 variables were named in the Mother Malaise data sets as follows:

- (1) Do you often have backache?  $(X_1)$
- (2) Do you feel tired most of the time?  $(X_2)$
- (3) Do you often feel depressed?  $(X_3)$
- (4) Do you often have bad headaches?  $(X_4)$
- (5) Do you often get worried about things?  $(X_5)$
- (6) Do you usually have great difficulty in falling or staying asleep?  $(X_6)$

- (7) Do you usually wake unnecessarily early in the morning?  $(X_7)$
- (8) Do you wear yourself out worrying about your health?  $(X_8)$
- (9) Do you often get into a violent rage?  $(X_9)$
- (10) Do people annoy and irritate you?  $(X_{10})$
- (11) Have you at times had a twitching of the face, head or shoulders?  $(X_{11})$
- (12) Do you suddenly become scared for no good reason?  $(X_{12})$
- (13) Are you scared to be alone when there are not friends near you?  $(X_{13})$
- (14) Are you easily upset or irritated?  $(X_{14})$
- (15) Are you frightened of going out alone or of meeting people?  $(X_{15})$
- (16) Are you constantly keyed up and jittery?  $(X_{16})$
- (17) Do you suffer from indigestion?  $(X_{17})$
- (18) Do you suffer from an upset stomach?  $(X_{18})$
- (19) Is your appetite poor?  $(X_{19})$
- (20) Does every little thing get on your nerves and wear you out?  $(X_{20})$
- (21) Does your heart often race like mad?  $(X_{21})$
- (22) Do you often have bad pain in eyes?  $(X_{22})$
- (23) Are you troubled with rheumatism or fibrosis?  $(X_{23})$
- (24) Have you ever had a nervous breakdown?  $(X_{24})$
- (25) Do you have other health problems?  $(X_{25})$

## 3 Potential Outcome Model

Let  $Y_{it}$  be the Rutter score derived variable for the *i*-th cohort member surveyed at the *t*-th sweep, and  $X_{1,it}, X_{2,it}, ..., X_{25,it}$  the mother malaise score derived variables for the *i*-th cohort member's parent (usually the mother) surveyed at the *t*-th sweep. Our linear panel data model without heterogeneity is introduced as follows.

$$Y_{it} = \beta_0 + \beta_1 X_{1,it} + \beta_2 X_{2,it} + \beta_3 X_{3,it} + \beta_4 X_{4,it} + \beta_5 X_{5,it} + \beta_6 X_{6,it} + \beta_7 X_{7,it} + \beta_8 X_{8,it} + \beta_9 X_{9,it} + \beta_{10} X_{10,it} + \beta_{11} X_{11,it} + \beta_{12} X_{12,it} + \beta_{13} X_{13,it} + \beta_{14} X_{14,it} + \beta_{15} X_{15,it} + \beta_{16} X_{16,it} + \beta_{17} X_{17,it} + \beta_{18} X_{18,it}$$
(1)  
$$+ \beta_{19} X_{19,it} + \beta_{20} X_{20,it} + \beta_{21} X_{21,it} + \beta_{22} X_{22,it} + \beta_{23} X_{23,it} + \beta_{24} X_{24,it} + \beta_{25} X_{25,it} + \varepsilon_{it}.$$

for i = 1, 2, ..., 3426, t = 1, 2, where  $\beta_{\cdot}$  is unknown parameter, and  $\varepsilon_{it}$  is an idiosyncratic error term assumed to be independent of the Rutter score derived variable and mother malaise score derived variables.

## 4 Bayesian Inference and Variable Selection

In the study, we consider quantile regression to estimate  $\beta$  from:

$$\min \sum_{i=1}^{3426} \sum_{t=1}^{2} \rho_p(Y_{it} - \sum_{j=1}^{25} \beta_j X_{j;it} - \beta_0),$$
(2)

where  $\rho_p(.)$  is the check function with

$$\rho_p(u) \equiv \{p - I(u < 0)\} \cdot u,\tag{3}$$

for 0 , where <math>I(.) is the indicator function. Instead of classical approach, a Bayesian approach and MCMC algorithm will be developed for posterior inference.

#### 4.1 Asymmetric Laplace Distribution

For a Bayesian analysis, the error term  $\varepsilon_{it}$  is assumed to follow the asymmetric Laplace distribution (ALD) with density

$$f_{AL}(\varepsilon_{it}) = \frac{p(1-p)}{\sigma} \exp\{-\rho_p(\frac{\varepsilon_{it}}{\sigma})\},\tag{4}$$

where  $\sigma$  is the scale parameter. For the properties of this distribution, see, for example, Yu and Moyeed (2001), Yu and Zhang (2005). Note that the *p*-th quantile of  $\varepsilon_{it}$  is zero,  $E(\varepsilon_{it}) = \frac{1-2p}{p(1-p)}$ , and  $Var(\varepsilon_{it}) = \frac{1-2p+2p^2}{p^2(1-p)^2}$ .

To develop MCMC algorithm for the quantile regression, a location scale mixture representation is applied:

$$\varepsilon_{it} = \theta v_{it} + \tau \sqrt{\sigma v_{it}} u_{it},\tag{5}$$

where  $\theta = \frac{1-2p}{p(1-p)}$ ,  $\tau = \frac{2}{p(1-p)}$ ,  $v_{it} \sim \varepsilon(\sigma)$  and  $u_{it} \sim N(0,1)$  are mutually independent random variables,  $\varepsilon(\sigma)$  is the exponential distribution with mean  $\sigma$  (Kozumi and Kobayashi, 2010). Thus the panel data model without heterogeneity is represented as follows.

$$Y_{it} = \beta_0 + \beta_1 X_{1,it} + \beta_2 X_{2,it} + \beta_3 X_{3,it} + \beta_4 X_{4,it} + \beta_5 X_{5,it} + \beta_6 X_{6,it} + \beta_7 X_{7,it} + \beta_8 X_{8,it} + \beta_9 X_{9,it} + \beta_{10} X_{10,it} + \beta_{11} X_{11,it} + \beta_{12} X_{12,it} + \beta_{13} X_{13,it} + \beta_{14} X_{14,it} + \beta_{15} X_{15,it} + \beta_{16} X_{16,it} + \beta_{17} X_{17,it} + \beta_{18} X_{18,it} + \beta_{19} X_{19,it} + \beta_{20} X_{20,it} + \beta_{21} X_{21,it} + \beta_{22} X_{22,it} + \beta_{23} X_{23,it} + \beta_{24} X_{24,it} + \beta_{25} X_{25,it} + \theta v_{it} + \tau \sqrt{\sigma v_{it}} u_{it},$$

$$(6)$$

where  $v_{it} \sim \varepsilon(\sigma)$  and  $u_{it} \sim N(0, 1)$  are mutually independent random variables.

To begin posterior inference, some prior distributions are supposed as follows: (1)  $\beta \sim N(\beta_0, B_0)$ , where  $\beta \equiv (\beta_0, \beta_1, ..., \beta_{25})$ , and  $\beta_0, B_0$  are specified parameters; (2)  $\sigma \sim IG(\frac{n_0}{2}, \frac{s_0}{2})$ , where IG(a, b) is the inverse Gamma distribution with the parameters a and b, and  $n_0, s_0$  are specified parameters; (3)  $\delta \sim N(\delta_0, D_0)$ , where  $\delta_0, D_0$  are specified parameters; (4)  $\varphi^2 \sim IG(\frac{m_0}{2}, \frac{r_0}{2})$ , where  $m_0, r_0$  are specified parameters. It is convenient to construct a MCMC algorithm.

#### 4.2 Markov Chain Monte Carlo Algorithm

A MCMC algorithm for the quantile regression is constructed by sampling  $\{v_{it}\}$ ,  $\beta$ ,  $\sigma$ , and  $\varphi^2$  from their full conditional distributions (Chib, 1992). A tractable and efficient Gibbs sampler is proposed as follows.

1. Sample  $v_{it}$  (i = 1, 2, ..., 3426; t = 1, 2) from  $\text{GIG}(\frac{1}{2}, \hat{c}_{it}^2, \hat{d}_{it}^2)$ , where

$$\hat{c}_{it}^2 = \frac{(Y_{it} - \beta^\top X_{it})^2}{t^2 \sigma},$$
(7)

$$\hat{d}_{it}^2 = \frac{\theta^2}{t^2\sigma} + \frac{2}{\sigma},\tag{8}$$

and  $\operatorname{GIG}(\nu, c, d)$  is the generalized inverse Gaussian distribution with the probability density function

$$f_{GIG}(x|\nu, c, d) = \frac{\left(\frac{d}{c}\right)^{\nu}}{2K_{\nu}(cd)} X^{\nu-1} \exp\{-\frac{1}{2}(c^2x^{-1} + d^2x)\},\tag{9}$$

for x > 0,  $-\infty < \nu < \infty$ , and c, d > 0, where  $K_{\nu}(.)$  is a modified Bessel function of the third kind (Barndorff-Nielsen and Shephard 2001).

2. Sample  $\beta$  from N( $\hat{\beta}, \hat{B}$ ), where

$$\hat{\beta} = \hat{B} \{ \sum_{i=1}^{3426} \sum_{t=1}^{2} \frac{(Y_{it} - \theta v_{it}) X_{it}}{t^2 \sigma v_{it}} + B_0^{-1} \beta_0 \},$$
(10)

$$\hat{B}^{-1} = \sum_{i=1}^{3426} \sum_{t=1}^{2} \frac{X_{it} X_{it}^{\top}}{t^2 \sigma v_{it}} + B_0^{-1}.$$
(11)

3. Sample  $\sigma$  from  $IG(\frac{\hat{n}}{2}, \frac{\hat{s}}{2})$ , where

$$\hat{n} = 20556 + n_0,\tag{12}$$

$$\hat{s} = \sum_{i=1}^{3426} \sum_{t=1}^{2} \frac{(Y_{it} - \beta^{\top} X_{it} - \theta v_{it})^2}{t^2 v_{it}} + 2 \sum_{i=1}^{3426} \sum_{t=1}^{2} v_{it} + s_0.$$
(13)

4. Sample  $\varphi^2$  from  $IG(\frac{\hat{m}}{2}, \frac{\hat{r}}{2})$ , where

$$\hat{m} = 3426 + m_0, \tag{14}$$

$$\hat{r} = \sum_{i=1}^{3426} \alpha_i^2 + r_0.$$
(15)

### 4.3 Marginal Likelihood

The marginal likelihood of the panel data model is defined as

$$m(Y) = \int f(Y|\eta)\pi(\eta)d\eta,$$
(16)

where  $f(Y|\eta)$  is the sampling density of the data  $\{Y\}$  and  $\pi(\eta)$  is the prior of the model specific parameter  $\eta$ .

The marginal likelihood can be reformulated as

$$m(Y) = \frac{f(Y|\eta)\pi(\eta)}{\pi(\eta|Y)},\tag{17}$$

from which it is suggested (Chib 1995) to estimate the marginal likelihood as follows.

$$\log m(Y) = \log f(Y|\eta^*) + \log \pi(\eta^*) - \log \pi(\eta^*|Y),$$
(18)

where  $\eta^*$  is a particular high density point, typically the posterior mean or mode.

For  $\eta \equiv \{\beta, \sigma, \varphi^2\}$  and  $Y \equiv \{Y_{it}\}$  in the panel data model, the posterior ordinate  $\pi(\eta^*|Y)$  is estimated by the following decomposition.

$$\pi(\eta^*|Y) = \pi(\sigma^*|Y)\pi(\beta^*|\sigma^*, Y)\pi(\varphi^{*2}|Y),$$
(19)

marginalized over the latent variables  $\alpha \equiv \{\alpha_i\}$  and  $v \equiv \{v_{it}\}$ , since the ordinates  $\pi(\sigma^*|Y)$ ,  $\pi(\beta^*|\sigma^*, Y)$ , and  $\pi(\varphi^{*2}|Y)$  can be estimated according to Chib (1995).

The likelihood ordinate  $f(Y|\eta^*)$  can be estimated by Chib method from

$$f(Y|\eta^*) = \frac{f(Y|\eta^*, \alpha^*)\pi(\alpha^*|\eta^*)}{\pi(\alpha^*|Y, \eta^*)},$$
(20)

where  $\alpha^*$  is the posterior mean of  $\alpha$ , and

$$f(Y|\eta^*, \alpha^*) = \sum_{i=1}^{3426} \sum_{t=1}^{2} f_{AL}(Y_{it} - \beta^{*\top} X_{it} - \beta_0 - \alpha_i^*), \qquad (21)$$

and

$$\pi(\alpha^*|\eta^*) = \frac{1}{2\pi\varphi^{*2}} \exp\{-\frac{\sum_{i=1}^{3426} \alpha_i^2}{2\pi\varphi^{*2}}\}.$$
(22)

And  $\pi(\alpha^*|Y, \eta^*)$  can be estimated from the output of a reduced Gibbs run with  $\eta$  fixed at  $\eta^*$ and sampling over  $\{\alpha, v\}$ .

#### 4.4 Variable Selection

To perform the variable selection for the quantile regression, an indicator vector is defined as follows.  $\gamma \equiv (\gamma_0, \gamma_1, ..., \gamma_{25})$ , where  $\gamma_0 = 1$ , and  $\gamma_i = 1$  for  $i \ge 2$  if  $\beta_i$  is included in the model ( $\beta_i \ne 0$ ), and  $\gamma_i = 0$  for  $i \ge 2$  if  $\beta_i$  is excluded in the model ( $\beta_i = 0$ ).

Given  $\gamma$ ,  $k_{\gamma}$  denote the size of the  $\gamma$ -th subset model,  $k_{\gamma} = \gamma^{\top} 1$ , and  $\beta_{k_{\gamma}}$  and  $X_{k_{\gamma},it}$  are  $k_{\gamma} \times 1$  vectors corresponding to all the components of  $\beta$  and  $X_{it}$  such that the corresponding  $\gamma_i$ 's are equal to 1. Given  $\gamma$ , the following prior assumptions are supposed.

- 1.  $\beta_{k_{\gamma}}|\sigma, \nu \sim \mathcal{N}(\beta_0, 2\sigma(X_{k_{\gamma}}^{\top}VX_{k_{\gamma}})^{-1})$ , where  $p(\sigma) \propto \sigma^{-1}$  and each  $\nu_i \sim \operatorname{Exp}\{\frac{\sigma}{p(1-p)}\}$ .
- 2. A prior distribution over model space  $\gamma$  is given by  $p(\gamma|\pi) \propto \pi^{k_{\gamma}} (1-\pi)^{k-k_{\gamma}}$ .
- 3.  $\pi \sim beta(a_0, b_0)$ .

Under the prior assumptions, a MCMC algorithm can be developed to compute posterior model probabilities in quantile regression by running the Gibbs sampler, and the marginal likelihood of Y under model  $\gamma$  can be obtained by integrating out  $\beta_{k\gamma}$  and  $\sigma$ ,

$$p(Y|\gamma,\nu,X) \propto \int p(\sigma)d\sigma \int p(Y|\beta_{k_{\gamma}},\gamma,\sigma,\nu,X)p(\beta_{k_{\gamma}}|\gamma,\sigma,\nu)p(\nu|\sigma)d\beta_{k_{\gamma}}.$$
 (23)

Integrating out  $\beta_{k_{\gamma}}$  and  $\sigma$  as a normal integral and an inverse gamma integral,

$$Y|\gamma,\nu,X \sim t_{(2n)}\{X_{k\gamma}\beta_0 + \xi\nu, \frac{1}{2}(V + VX_{k\gamma}(X_{k\gamma}^{\top}VX_{k\gamma})^{-1}X_{k\gamma}^{\top}V)\}.$$
(24)

Then, the Gibbs sampler can be implemented to generate samples of

$$p(Y|\gamma,\nu,X) \propto p(Y,\gamma,\nu,X)p(\gamma|\pi).$$
 (25)

### 5 Real Data Application

In this section, the Bayesian quantile regression is applied to analysis the British Cohort study data. This data set was extensively investigated for many sorts of topics, but this paper examines the influence of maternal health problems on child's worrying status. There are 3426 observations, 25 predictor variables, and one response variable. We assume a quantile regression model between the response variable and the 25 covariates, plus an intercept.

In Table 1, upon Bayesian quantile regression applying the MCMC package in R, the

model is evaluated at three different quantiles 0.05, 0.5 and 0.95. The maternal health problems have different influence on child's worrying status at different quantiles, through MCMC quantile regression iteration 50001 of 51000, in detail,  $\beta_i$  have different estimates at different quantiles for each i = 0, ..., 25.  $\beta_{24}$  and  $\beta_{25}$  have the biggest absolute value for the three quantiles, except for  $\beta_0$ .

Table 2 describes the summary at the quantile 0.05 aplying Bayesian quantile regression through the MCMC package in R. Upon Bayesian quantile regression applying the MCMC package in R, Table 3 sumarizes the empirical mean and standard deviation for each variable  $X_i$  (i = 1, ..., 25), and standard error of the mean for the model at the quantile 0.05. In this case,  $X_{24}$  has the biggest standard deviation, and  $X_{25}$  has the next biggest standard deviation. Upon Bayesian quantile regression at the quantile 0.05 applying the MCMC package in R, Table 4 sumarrizes the quantiles for each variable  $X_i$  (i = 1, ..., 25).

Tables 5-7 sumarrizes the same contents for the quantile 0.50, and Tables 8-10 for the quantile 0.95.

Applying the stochastic search variable selection, the top models and the posterior model probabilities are summerized in Table 11-13 for the different quantiles 0.05, 0.5 and 0.95. The maternal nervous breakdown,  $X_{24}$ , among the 25 maternal health problems, contributed most to child's worrying status for the three different quantiles, and the maternal other health problems,  $X_{25}$ , contributed the next most. At the quantile 0.05, maternal often feel depressed,  $X_3$ , contributed the third most, while maternal feel tired most of the time,  $X_2$ , contributed respectively the third and fourth most at the quantile 0.50 and 0.95.

## 6 Conclusions

In this paper, we developed a Bayesian quantile regression on linear panel data model without heterogeneity, in particular, upon a location-scale mixture representation of the asymmetric Laplace error distribution, this paper provides how the posterior distribution can be sampled and summarized by MCMC method.

In addition, the influence of maternal health problems on child's worrying status was estimated applying the 1970 BCS data, and we find that maternal's different health problem has different influence on child's worrying status at different quantiles, also that maternal nervous breakdown, in our method, among the 25 maternal health problems, contributes most to influence the child's worrying status.

Our findings have high policy relevance in terms of the importance of the intervention of maternal nervous breakdown early for the influence on child's worrying statuts.

## References

Barndorff-Nielsen, O. E. and N. Shephard, (2001), Non-Gaussian Ornstein-Uhlenbeck-based models and some of their uses in financial economics, *J. Royal Stat. Soc.* Series B (63): 167-241.

Blanden, J., P. Gregg and L. Macmillan (2007), Accounting for intergenerational income persistence: noncognitive skills, ability and education, *Econom. J.* **117**: C43-C60.

Buchinsky, M. (1998), Recent advances in quantile regression models: a practical guideline for empirical authors, *J. Hum Resour.* **33**: 88-126.

Chib, S. (1992), Bayes inference in the Tobit censored regression model, J. Econom. 51: 79-99.

Chib, S. (1995), Marginal likelihood from the Gibbs output, J. Amer. Stat. Assoc. 90: 1313-1321.

Chib, S. (2001) Markov chain Monte Carlo methods: computation and inference, *In: Heck*man J. J., Leamer E (eds) Handbook of econometrics, North-Holland, Amsterdam 5: 3569-3649.

Conti, G. and J. Heckman (2010), Understanding the Early Origins of the Education Health Gradient, *Persp. Psych. Sci.* 5: 585-605.

Cutler, D. and A. Lleras-Muney (2010), Understanding differences in health behaviors by education, *J. Heal. Econom.* **29**: 1-28.

Feinstein, L. (2000), The Relative Economic Importance of Academic, Psychological and Behavioural Attributes Developed on Chilhood, *CEP Discuss. Pap.*. Frühwirth-Schnatter, S. and H. F. Lopes (2009), Parsimonious Bayesian Factor Analysis when the Number of Factors is Unknown, *Unpub. Tech. Repo.*.

Gamerman, D. and H. F. Lopes (2006), Markov ChainMonte Carlo: Stochastic simulation for Bayesian inference (2nd ed), *Chapman and Hall/CRC, Boca Raton*.

Guo, M. and W. Härdle (2012), Simultaneous confidence bands for expectile functions, *Adv. Stat. Anal.* **96** : 517-542.

Hanson, T. and W. O. Johnson(2002), Modeling regression error with a mixture of Pölya trees, *J Amer. Stat. Assoc.* **97**: 1020-1033.

Hampson, S. E. and H. S. Friedman (2008), Personality and Health: A Lifespan Perspective, in The Handbook of Personality: Theory and Research, ed. by O. P. John, R. Robins, and L. Pervin, New York: Guilford (third ed): 770-794.

Härdle, Wolfgang K. and Song Song (2010), Confidence Bands In Quantile Regression, *Econometr. Th.* **26** (04): 1180-1200.

Heckman, J. J., J. Stixrud and S. Urzua (2006), The Effects of Cognitive and Noncog-nitive Abilities on Labor Market Outcomes and Social Behavior, *J. Lab. Econom.* **24**: 411-482.

Kaestner, R. and K. Callison (2011), Adolescent Cognitive and Noncognitive Correlates of Adult Health, *J. Hum. Capti.* 5: 29-69.

Koenker, R. (2005), Quantile regression, Camb. Univ. Pr., New York.

Kottas, A. and A. E. Gelfand (2001), Bayesian semiparametric median regression modeling,J. Amer. Stat. Assoc. 96: 1458-1468.

Kottas, A. and M. Krnjajic (2009), Bayesian semiparametric modelling in quantile regression, *Scand. J. Stat.* **36**: 297-319.

Kozumi, H. and G. Kobayashi (2010), Gibbs sampling methods for Bayesian quantile regression, J. Stat. Comput. Simul. 81: 1565-1578.

Liu, J. S. (2001), Monte Carlo Strategies in scientific computing, Springer, New York.

Murasko, J. E. (2007), A lifecourse study on education and health: The relationship between childhood psychosocial resources and outcomes in adolescence and young adulthood, *Soc. Sci. Res.* **36**: 1348-1370.

Reich, B. J., H. D. Bondell and H. Wang(2010), Flexible Bayesian quantile regression for independent and clustered data, *Biostat.* **11**: 337-352.

Roberts, B. W., P. Harms, J. L. Smith, D. Wood, and M. Webb (2006), Using Multiple Methods in Personality Psychology, in Handbook of Multimethod Measurement in Psychology, ed. by M. Eid and E. Diener, Washington, D.C.: Ame. Psych. Assoc.: 321-335.

Roberts, B. W., N. R. Kuncel, R. L. Shiner, A. Caspi, and L. R. Goldberg (2007), The power of personality: The comparative validity of personality traits, socioeconomic status, and cognitive ability for predicting important life outcomes, *Persp. Psych. Sci.* **2**: 313-345.

Schnabel, S. and P. Eilers (2009a), An analysis of life expectancy and economic production using expectile frontier zones, *Demogr. Res.* **21**: 109-134.

Schnabel, S. and P. Eilers (2009b), Optimal expectile smoothing, *Comput. Stat. Data Anal.*53: 4168-4177.

Taddy, M. A. and A. Kottas (2010), A Bayesian nonparametric approach to inference for quantile regression, *J. Bus. Econ. Stat.* **28**: 357-369.

Taylor, J. (2008), Estimating value at risk and expected shortfall using expectiles, J. Finan.Economet. 6: 231-252.

Tsionas, E. G. (2003), Bayesian quantile inference, J. Stat. Comput. Simul. 73: 659-674.

Walker, S. G. and B. K. Mallick (1999), A Bayesian semiparametric accelerated failure time model, *Biomet.* 55: 477-483.

Yu, K. (2002), Quantile regression using RJMCMC algorithm, Comput. Stat. Data Anal.40: 303-315.

Yu, K. and R. A. Moyeed (2001), Bayesian quantile regression, *Stat. Probab. Lett.* **54**: 437-447.

Yu, K. and J. Stander (2007), Bayesian analysis of a Tobit quantile regression model, *J. Econom.* **137**: 260-276.

Yu, K., Z. Lu and J. Stander (2003), Quantile regression: applications and current research area, *Stat.* **52**: 331-350.

Yu, K. and J. Zhang (2005), A Three-Parametric Asymmetric Laplace Distribution and Its Extension, *Comm. Stat. Th. Meth.* **34**: 1867-1879.

Yuan, Y. and G. Yin (2010), Bayesian quantile regression for longitudinal studies with nonignorablemissing data, *Biomet.* **66**: 105-114.

Yue, Y. R. and H. Rue (2011), Bayesian inference for additive mixed quantile regression models, *Comput. Stat. Data Anal.* **55**: 84-96.

Zwick, W. R. and W. F. Velicer (1986), Comparison of Five Rules for Determining the Number of Components to Retain, *Psych. Bull.* **99**: 432-442.

## 7 Appendix: Tables

	q = 0.05	q = 0.50	q = 0.95
$\beta_0$	1126.80	2909.93	6219.29
$\beta_1$	5.13	0.56	0.95
$\beta_2$	-3.30	0.05	-8.85
$\beta_3$	0.23	-0.41	-0.30
$\beta_4$	-1.11	0.25	-3.58
$\beta_5$	-4.88	-0.09	0.93
$\beta_6$	-0.10	-0.20	-2.80
$\beta_7$	2.20	-0.55	-3.76
$\beta_8$	-1.81	2.09	1.86
$\beta_9$	-0.41	-1.19	-5.94
$\beta_{10}$	2.22	0.28	0.06
$\beta_{11}$	-14.86	-3.09	-7.68
$\beta_{12}$	-13.23	-0.79	-2.01
$\beta_{13}$	13.86	0.79	6.21
$\beta_{14}$	0.96	0.27	5.51
$\beta_{15}$	6.42	1.49	-6.35
$\beta_{16}$	2.87	0.41	-5.71
$\beta_{17}$	2.75	0.54	3.07
$\beta_{18}$	-0.85	-0.38	3.42
$\beta_{19}$	-3.20	0.32	2.77
$\beta_{20}$	6.24	-1.07	1.86
$\beta_{21}$	4.43	0.74	3.21
$\beta_{22}$	1.31	0.50	0.54
$\beta_{23}$	-3.54	0.10	-5.09
$\beta_{24}$	-194.69	63.94	317.94
$\beta_{25}$	79.96	-40.22	-289.67

Table 1:  $\beta$  for the quantile q=0.05, 0.50, 0.95 (MCMC quantreg iteration 50001 of 51000, and all figures e-3 units)

Iterations = 1001 : 50991	Thinning interval $= 10$
Number of chains $= 1$	Sample size per chain $= 5000$

Table 2: Summary (posterior) for the quantile q=0.05

	Mean	SD	Naive SE	Time-series SE
(Intercept)	80960.000	71879.300	1017.000	1106.000
$X_1$	261.900	213.400	3.018	3.491
$X_2$	-149.800	237.600	3.360	3.822
$X_3$	185.400	340.400	4.814	5.271
$X_4$	-75.700	245.800	3.476	3.877
$X_5$	-254.900	257.300	3.638	4.211
$X_6$	-157.500	267.900	3.789	3.952
$X_7$	163.800	273.500	3.868	4.166
$X_8$	-186.800	461.000	6.519	7.460
$X_9$	-6554.000	335.300	4.742	5.084
$X_{10}$	1507.000	290.300	4.106	4.513
$X_{11}$	-313.300	557.300	7.881	8.479
$X_{12}$	-329.200	533.100	7.539	8.646
$X_{13}$	38.260	472.600	6.684	7.343
$X_{14}$	-4.005	288.400	4.079	4.303
$X_{15}$	237.800	352.400	4.984	5.331
$X_{16}$	49.760	423.700	5.992	6.617
$X_{17}$	-163.300	379.400	5.365	6.031
$X_{18}$	4.134	425.900	6.023	6.681
$X_{19}$	188.400	383.400	5.423	5.706
$X_{20}$	200.100	429.500	6.074	6.698
$X_{21}$	511.500	445.400	6.298	7.015
$X_{22}$	-145.200	456.700	6.459	6.873
$X_{23}$	50.030	266.600	3.771	3.990
$X_{24}$	8781.000	29472.100	416.800	449.800
$X_{25}$	894.100	15204.000	215.000	225.300

Table 3: Empirical mean and standard deviation for each variable, and standard error of the mean for the quantile q=0.05 (all figures e-3 units)

	2.5%	25%	50%	75%	97.5%
$\overline{X_1}$	-1.34700	1.13700	2.54300	3.98620	6.93500
$X_2$	-6.33800	-3.0220	-1.45200	0.12610	3.02100
$X_3$	-4.75700	-0.49200	1.84600	4.15660	8.71300
$X_4$	-5.81500	-2.35300	-0.73510	0.89110	3.99100
$X_5$	-7.70100	-4.26700	-2.55100	-0.78220	2.43500
$X_6$	-6.94900	-3.34100	-1.56900	0.25070	3.75800
$X_7$	-3.83500	-0.13280	1.64700	3.46200	7.04700
$X_8$	-10.26800	-5.08700	-2.13500	1.18830	7.48600
$X_9$	-7.25500	-2.92700	-0.70160	1.57420	6.00400
$X_{10}$	-5.59700	-1.81500	0.23440	2.10240	5.73600
$X_{11}$	-13.57600	-6.94100	-3.33700	0.59920	8.25000
$X_{12}$	-13.38400	-6.96400	-3.31500	0.28870	7.30000
$X_{13}$	-8.44000	-2.85800	0.24870	3.44650	10.18400
$X_{14}$	-5.73800	-1.93200	-0.06721	1.90910	5.67600
$X_{15}$	-3.93900	-0.09158	2.16200	4.58360	9.75500
$X_{16}$	-7.83700	-2.42900	0.44340	3.29010	8.77200
$X_{17}$	-9.35300	-4.09600	-1.53500	0.91150	5.69400
$X_{18}$	-8.17500	-2.86500	-0.01683	2.891103	8.58500
$X_{19}$	-5.68900	-0.60500	1.91100	4.39410	9.39800
$X_{20}$	-6.46200	-0.87610	1.97500	4.88770	10.38500
$X_{21}$	-3.12100	2.08200	4.94800	7.97480	14.39400
$X_{22}$	-10.27300	-4.54000	-1.46500	1.52430	7.74900
$X_{23}$	-4.87600	-1.25900	0.54290	2.24970	5.87200
$X_{24}$	-475.64400	-100.40000	74.99000	264.89090	698.47500
$X_{25}$	-292.12600	-91.20000	7.40400	108.54190	310.32500

Table 4: Quantiles for each variable when the quantile q=0.05 (all figures e-3 units)

Iterations = 1001 : 50991	Thinning interval $= 10$
Number of chains $= 1$	Sample size per chain $= 5000$

Table 5: Summary (posterior) for the quantile q=0.50

	Mean	SD	Naive SE	Time-series SE
(Intercept)	29510.00000	1917.03100	27.11000	27.11000
$X_1$	0.66020	4.70700	0.06656	0.06889
$X_2$	0.42350	4.45500	0.06300	0.06300
$X_3$	2.91500	7.11300	0.10060	0.10060
$X_4$	-1.09500	4.83300	0.06835	0.06898
$X_5$	-1.02500	4.17200	0.05899	0.05899
$X_6$	-0.02617	6.51800	0.09217	0.09471
$X_7$	-1.56800	6.86200	0.09704	0.09704
$X_8$	2.16700	12.10100	0.17110	0.17110
$X_9$	-1.96000	7.36500	0.10420	0.10420
$X_{10}$	-45.60000	5.74800	0.08129	$0.0 \ 8129$
$X_{11}$	-5.42100	13.93300	0.19700	0.19700
$X_{12}$	-6.85000	12.46000	0.17620	0.17250
$X_{13}$	2.50500	12.51200	0.17700	0.17700
$X_{14}$	-1.28200	6.02300	0.08517	0.08517
$X_{15}$	1.26500	9.32900	0.13190	0.13190
$X_{16}$	1.27600	9.62700	0.13610	0.13810
$X_{17}$	-0.27990	7.54500	0.10670	0.10670
$X_{18}$	2.56600	9.28200	0.13130	0.13130
$X_{19}$	1.81300	11.09900	0.15700	0.15350
$X_{20}$	-4.30400	10.52200	0.14880	0.14880
$X_{21}$	2.18700	11.71400	0.16570	0.16950
$X_{22}$	3.21700	9.07700	0.12840	0.11980
$X_{23}$	1.50600	6.13100	0.08671	0.08671
$X_{24}$	489.50000	832.31100	0.11770	11.7700
$X_{25}$	-172.10000	360.37700	5.09600	5.09600

Table 6: Empirical mean and standard deviation for each variable, and standard error of the mean for the quantile q=0.50 (all figures e-4 units)

	2.5%	25%	50%	75%	97.5%
(Intercept)	25445.4100	28376.7290	29630.0000	30743.89190	33003.4600
$X_1$	-8.6250	-2.4480	0.5838	3.6300	10.1710
$X_2$	-8.5120	-2.4630	0.4258	3.2990	9.3610
$X_3$	-10.8590	-1.7350	2.7430	7.4820	17.5130
$X_4$	-11.0650	-4.2140	-1.1040	2.0350	8.1710
$X_5$	-9.8440	-3.6330	-0.8936	1.6830	7.0560
$X_6$	-12.7880	-4.2380	-0.0366	4.2310	12.7960
$X_7$	-15.3660	-5.8820	-1.4430	3.0750	11.6360
$X_8$	-21.2970	-5.3980	2.0210	9.5740	26.5670
$X_9$	-16.9570	-6.6250	-1.9170	3.0030	12.1740
$X_{10}$	-12.1040	-4.0950	-0.2667	3.3190	10.6870
$X_{11}$	-33.8050	-14.5850	-4.8640	3.8510	21.6330
$X_{12}$	-34.0110	-14.3300	-6.1220	1.5110	16.1080
$X_{13}$	-22.5280	-5.1120	2.2030	9.8840	27.8070
$X_{14}$	-13.8990	-5.0690	-1.1530	2.6480	10.1430
$X_{15}$	-16.8440	-4.6930	1.0780	7.0880	20.4560
$X_{16}$	-17.3840	-5.0210	1.0840	7.3910	20.8090
$X_{17}$	-15.8120	-4.9400	-0.2400	4.6070	14.7560
$X_{18}$	-15.0820	-3.3770	2.3710	8.3070	21.7620
$X_{19}$	-19.4420	-5.2890	1.5910	8.5320	25.0950
$X_{20}$	-26.2960	-11.1120	-4.0050	2.6800	15.8220
$X_{21}$	-21.3700	-5.5090	2.1500	9.5880	25.7640
$X_{22}$	-14.1720	-2.7470	3.0950	9.0090	21.8540
$X_{23}$	-10.5890	-2.4880	1.3630	5.4100	13.9490
$X_{24}$	-968.4610	-48.3330	402.5000	955.8340	2391.5660
$X_{25}$	-927.5700	-399.4760	-156.6000	68.2750	502.9410

Table 7: Quantiles for each variable when the quantile q=0.50 (all figures e-4 units)

Iterations = 1001 : 50991	Thinning interval $= 10$
Number of chains $= 1$	Sample size per chain $= 5000$

Table 8: Summary (posterior) for the quantile q=0.95

	Mean	SD	Naive SE	Time-series SE
(Intercept)	543695.460	89426.900	1265.000	1526.000
$X_1$	-26.660	263.000	3.720	4.410
$X_2$	-315.410	285.900	4.044	5.278
$X_3$	56.890	380.900	5.387	6.252
$X_4$	-272.060	277.500	3.924	4.794
$X_5$	-188.940	267.000	3.776	4.756
$X_6$	209.250	330.700	4.677	5.667
$X_7$	-219.800	321.400	4.546	5.336
$X_8$	114.880	493.900	6.985	7.819
$X_9$	-323.280	383.700	5.426	6.256
$X_{10}$	-23.130	344.300	4.869	5.876
$X_{11}$	107.880	587.300	8.305	9.311
$X_{12}$	-288.510	506.800	7.167	7.714
$X_{13}$	-182.250	502.800	7.111	7.820
$X_{14}$	-119.030	348.300	4.925	5.872
$X_{15}$	-180.200	426.800	6.036	7.686
$X_{16}$	45.020	449.200	6.353	7.070
$X_{17}$	46.290	382.700	5.412	6.318
$X_{18}$	40.220	451.800	6.389	7.439
$X_{19}$	-283.000	463.500	6.555	7.313
$X_{20}$	-340.210	457.600	6.472	7.280
$X_{21}$	5380.900	451.000	6.378	7.051
$X_{22}$	596.060	476.700	6.742	7.828
$X_{23}$	-69.550	327.200	4.627	5.620
$X_{24}$	11901.210	32910.100	465.400	526.100
$X_{25}$	-17966.530	18277.500	258.500	324.300

Table 9: Empirical mean and standard deviation for each variable, and standard error of the mean for the quantile q=0.95 (all figures e-5 units)

	2.5%	25%	50%	75%	97.5%
(Intercept)	3783.021000	4822.00000	5411.14290	6011.00000	7310.98700
$X_1$	-5.526000	-2.044000	-0.182300	1.547000	4.797000
$X_2$	-8.516000	-5.127000	-3.207600	-1.260000	2.565000
$X_3$	-7.097000	-2.014000	0.679300	3.184000	7.869000
$X_4$	-8.036000	-4.580000	-2.731600	-79.930000	2.706000
$X_5$	-7.234000	-3.644000	-1.910700	-705.400000	3.189000
$X_6$	-4.811000	-0.073560	2.210700	4.391000	8.246000
$X_7$	-8.675000	-4.335000	-2.161400	0.007187	3.938000
$X_8$	-8.859000	-2.114000	1.186400	4.435000	10.403000
$X_9$	-10.886000	-5.801000	-3.227300	-0.648600	4.243000
$X_{10}$	-7.099000	-2.538000	-0.192100	2.090000	6.376000
$X_{11}$	-11.012000	-2.672000	1.329400	5.071000	11.764000
$X_{12}$	-13.181000	-6.219000	-2.721400	0.581100	6.605000
$X_{13}$	-12.166000	-5.053000	-1.754700	1.648000	7.593000
$X_{14}$	-8.183000	-3.535000	-1.173300	1.203000	5.571000
$X_{15}$	-10.492000	-4.647000	-1.685700	1.147000	6.205000
$X_{16}$	-8.687000	-2.559000	0.555000	3.577000	8.928000
$X_{17}$	-7.463000	-2.024000	0.643100	3.161000	7.391000
$X_{18}$	-8.881000	-2.501000	0.658700	3.484000	8.691000
$X_{19}$	-12.285000	-5.818000	-2.713800	0.417100	5.652000
$X_{20}$	-12.563000	-6.433000	-3.268300	-0.329300	5.214000
$X_{21}$	-4.353000	2.590000	5.707900	8.514000	13.439000
$X_{22}$	-3.864000	2.872000	6.214400	9.278000	14.778000
$X_{23}$	-7.358000	-2.825000	-0.538400	1.571000	5.350000
$X_{24}$	-90.350000	-88.010000	147.516800	49.500000	696.594000
$X_{25}$	-555.750000	-300.300000	-172.533700	-49.340000	153.451000

Table 10: Quantiles for each variable when the quantile q=0.95 (all figures e-3 units)

Models	Probability
(Intercept)	0.9278
$X_{24}$	0.0502
(Intercept), $X_{24}$	0.0142
(Intercept), $X_{25}$	0.0052
(Intercept), $X_3$	0.0004

Table 11: Variable Selection for the quantile q=0.05 (SSVS quantreg iteration 50001 of 51000)

Models	Probability
(Intercept)	0.9954
(Intercept), $X_{24}$	0.0040
(Intercept), $X_{25}$	0.0004
(Intercept), $X_2$	0.0002

Table 12: Variable Selection for the quantile q=0.50 (SSVS quantreg iteration 50001 of 51000)

Models	Probability
(Intercept)	0.9274
(Intercept), $X_{24}$	0.0486
(Intercept), $X_{25}$	0.0146
(Intercept), $X_{20}$	0.0012
(Intercept), $X_2$	0.0010

Table 13: Variable Selection for the quantile q=0.95 (SSVS quantreg iteration 50001 of 51000)

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